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13. ABSTRACT (Maximum 200 words) This grant is supporting development of mathematical foundations for sensor management systems. This year's accomplishments are in three areas: Extension of a Kalman-filter based discrimination metric to interacting multiple model filters; extension of sensor management based on Joint Multitarget Probabilities to incorporate multiple sensor modes and target classification; and development of fast methods to solve the Fokker-Planck equation for real-time non-linear filtering applications. To support sensor management representations of multi-target probability densities must be developed that model the uncertainty between quantities such as the number of targets, their locations and their class. To solve this problem and study it in a simple setting, the notion of Joint Multitarget Probabilities for detection, tracking, and target classification was developed and tested. In certain cases the time-evolution of these probabilities is characterized by a partial differential equation called the Fokker-Planck equation leading to a nonlinear filter. Several prototype nonlinear filters using the Alternating Direction Implicit scheme to solve the Fokker-Planck equation in real-time were formulated. In these applications it seems to offer significant improvement in estimation performance at a supportable cost in computational load.				
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1997 Progress Report for AFOSR

## **Sensor Management Research**

Grant Number: AFOSR/F49620-96-1-0382

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**1. Objectives:** This project is developing mathematical foundations for sensor management systems. Sensor management can be viewed as the process of selecting sensors, sensor modes and sensor dwell points to optimize the probability density characterizing a set of targets in a region. Thus, there are two parts to this problem. In order to support this approach, representations of multitarget probability densities must be developed that are rich enough to model the uncertainty between quantities such as the number of targets in a region, their locations and target classes. Then, given this probability density, measures of sensor effectiveness must be computed and optimized. This work is a collaboration between Lockheed-Martin Tactical Defense Systems, the Minnesota Center for Industrial Mathematics (MCIM) and Mr. S. Musick at the USAF Wright Laboratory.

**2. Status of Effort:** Sensor management requires optimizing sensor effectiveness across multiple conflicting objectives such as a desire to localize and classify known targets while attempting to detect new ones as well. This requires joint representation of the probability density for the number, location and class of a collection of targets. In order to solve this problem and to study it in a simple setting, we developed the notion of Joint Multitarget Probabilities for detection and tracking. During the past year this was extended to the problem of sensor management with target classification.

A related issue that arises in this context is determining how these probability densities evolve in time. The resulting densities are often very complicated. Even in single target cases, determining the time evolution of these densities is a challenge requiring new algorithmic approaches. In certain cases this evolution is characterized by a partial differential equation called the Fokker-Planck equation (FPE) and its generalizations. Although this has long been known, solution of the FPE has generally been regarded as unfeasible for real-time applications. Now, recent advances in computers and numerical methods may have changed this. To explore the viability of real-time FPE solutions, we developed several solution schemes and applied them to test problems with very promising results.

Some of our past work on sensor management for multitarget/multisensor developed discrimination gain for the case of a collection of targets described by conventional Kalman filters. In a generalization of this work, a method for computing the expected discrimination gain was developed for multiple model Kalman filters. This is being applied in a more realistic setting under a transitioning Small Business Innovative Research program.

**3. Accomplishments:** This year's accomplishments are in three areas: Extension of a Kalman-filter based discrimination metric for sensor management to a more general class of filters; extension of sensor management based on Joint Multitarget Probabilities to incorporate multiple sensor modes and target classification; and the development of fast

methods to solve the Fokker-Planck equation for real-time non-linear filtering applications.

Expected discrimination gain is a useful general measure of sensor effectiveness that was developed for targets being tracked by Kalman filters. Real applications often require more sophisticated filters which characterize target motion in terms of both continuous dynamical states and discrete states referred to as dynamics modes. A measure of discrimination gain was derived to apply to this case [6]. In this case, there are two factors that contribute to the expected discrimination gain: the reduction in uncertainty about the target's kinematics; and the reduction in the uncertainty about the target's flight mode, e.g. whether the target is turning or in straight and level flight.

Earlier work on discrimination gain for static detection problems [1] was generalized to the problem of dynamic targets and dynamic targets with classification and sensors with multiple modes to select from [7]. In this case, discrimination can be optimized by determining where to direct the sensors and which sensor mode to use. For example, in a test problem with a sensor that can either detect or classify targets, discrimination is initially optimized by using the sensor in its detection mode. After the targets have been detected and localized the classification mode begins to have high discrimination value.

In order to compute the expected discrimination gain when a sensor mode and dwell point is selected, the time evolution of the probability density between measurements must be computed. This can be determined by the Fokker-Planck equation FPE (or closely related equations). In collaboration with researchers at the U. of MN we explored several methods for solving the FPE in real time. With Dr. M. Kouritzin, a convolution-based scheme for altitude tracking was developed and evaluated [8]. Several techniques for solution of the FPE using finite difference schemes were explored. As part of his Master's degree work at the Minn. Center for Industrial Mathematics, Mr. A. Zatezelo developed and tested four FPE solvers against a model problem typifying tracking applications. Dr. Kastella supervised this work while Mr. Zatezelo interned with LMTDS-E in the summer of '96. Dr. N. Krylov is Mr. Zatezelo's advisor. Valuable insight into the proper way to treat the boundary condition for this type of problem was provided by Prof. Friedman. The four FPE solvers we studied were: the Alternating Direction Implicit (ADI) scheme; the method of fractional steps; an Euler explicit scheme; and a multigrid scheme. For this problem ADI and the method of fractional steps were found to be about two orders of magnitude more efficient than the Euler explicit and multigrid schemes.

Based on this study, the Alternating Direction Implicit (ADI) scheme seems very promising for sensor management and non-linear filtering applications. ADI is a so-called  $O(N)$  algorithm, which means that its computational complexity grows linearly with the size of the finite-element grid used to discretize the problem. In an effort to assess the feasibility of ADI-based non-linear filtering, a diverse set of model applications have been formulated. These model applications are: 1) low-SNR image tracking with nonlinear target dynamics and non-Gaussian measurements [4]; 2) missile altitude

tracking with severe multipath interference [3] and; 3) joint tracking and identification using RADAR position measurements and range-profile measurements [5] (suggested by Mr. S. Musick, USAF-WL). This work is currently being summarized in a series of papers [2-5]. In all three applications, NLF seems to offer significant improvement in estimation performance at a supportable cost in computational load. For example, in low-signal/noise ratio image tracking, the NLF seems to provide an order of magnitude improvement in performance against maneuvering targets. In simulation tests for tracking in multipath interference, NLF successfully tracks targets that are essentially untrackable by other means. In the joint tracking and classification problem, NLF reduces the time to classify the target by about 50%, compared to a direct maximum-likelihood classifier.

#### **4. Personnel Supported:**

Avner Friedman

Keith Kastella

Wayne Schmaedeke

#### **5. Technical Publications:**

Journal Publications:

1. K. Kastella, "Discrimination Gain to Optimize Detection and Classification", IEEE Systems, Man and Cybernetics, Jan. 1997
2. A. Zatezelo, K. Kastella, "Solution Schemes for Real-Time Nonlinear Filtering", in preparation
3. K. Kastella, A. Zatezelo, "A Nonlinear Filter for Low-elevation Target Tracking in Multipath", in preparation.
4. K. Kastella, A. Zatezelo, "A Nonlinear Filter for Low-SNR Maneuvering Target Detection and Tracking", in preparation.
5. K. Kastella, A. Zatezelo, "A Nonlinear Filter for Joint Tracking and Identification", in preparation.
6. W. Schmaedeke, K. Kastella, "Discrimination Based Sensor Management with Interacting Multiple Model Filters", in preparation.

Reviewed Conference Proceedings

7. K. Kastella, "Joint Multitarget Probabilities for Detection and Tracking", K. Kastella, SPIE AeroSense '97

8. K. Kastella, M.A. Kouritzin, and A. Zatezalo, "A Nonlinear Filter for Altitude Tracking", 1996 Proceedings of the Air Traffic Control Association

## **6. Interactions/Transitions:**

### **6.1 Conference Presentations:**

K. Kastella, A. Zatezalo, "Nonlinear Filtering for Detection, Tracking and ID Algorithms", ONR Filtering and Tracking Workshop, Dahlgren, VA, May, 1997

Presentation to Naval Surface Warfare Center:

K. Kastella, "Discrimination based sensor management for detection, tracking and classification", - Dahlgren, May, 1997

### **6.2 Transitions:**

An algorithm using discrimination-based sensor management with Interacting Multiple Model Kalman Filters (IMMKF) is currently being incorporated into a Phase I Small Business Innovative Research (SBIR) contract called "Sensor Management Across Multiple Platforms (SMAMPS)".

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## **7. Patent Disclosures**

None

## **8. Honors**

None